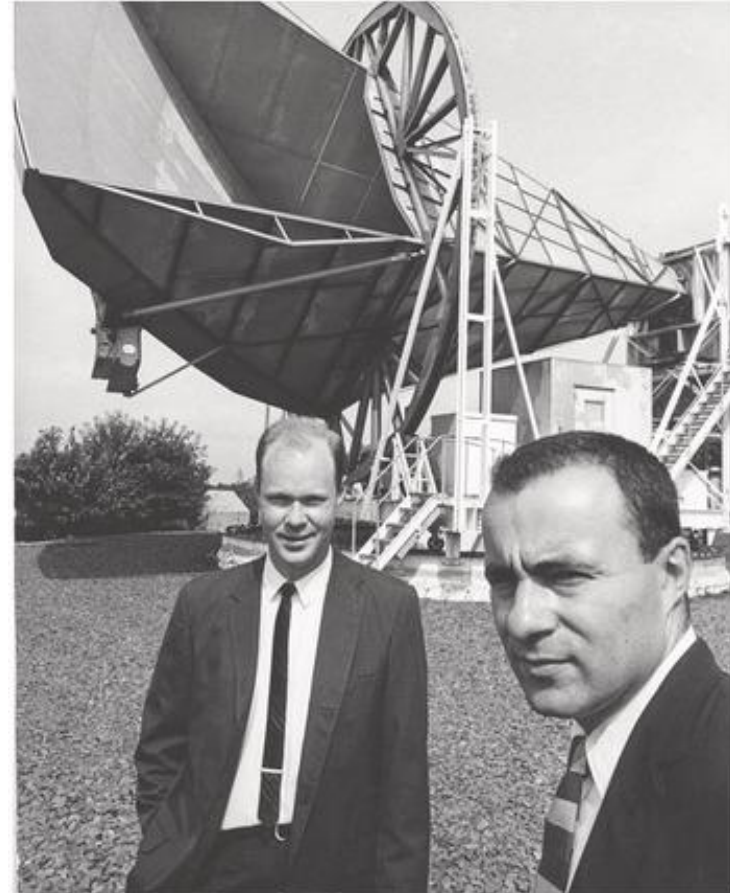
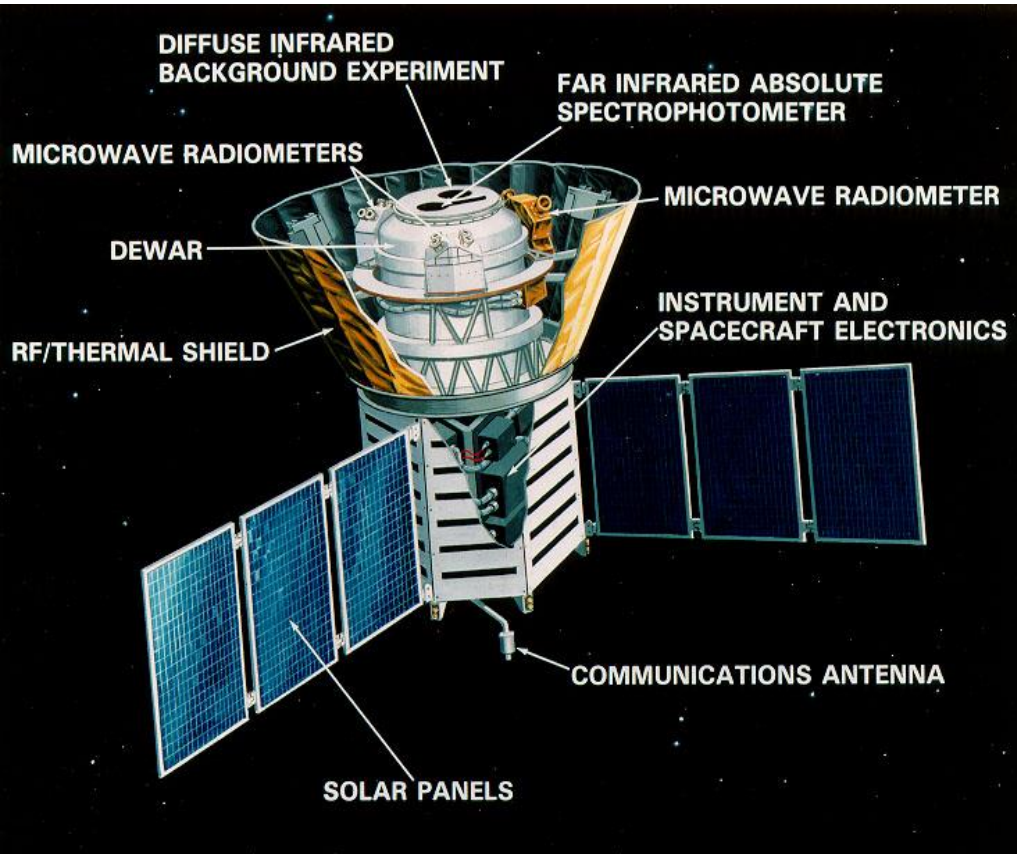


Discovery of the Cosmic Microwave Background (CMB)

- Early signs and speculations in the 1940s
- Arno Penzias & Robert Wilson
 - 1964 discovery using a 6 m horn antenna at Bell Labs, New Jersey
 - published in 1965 with interpretation by Robert H. Dicke, Jim Peebles, and David Wilkinson at Princeton University
 - Nobel Prize in 1978
- Developments in theory in the 1970s
- 1989-1993 operation of the NASA *Cosmic Background Explorer (COBE)* satellite



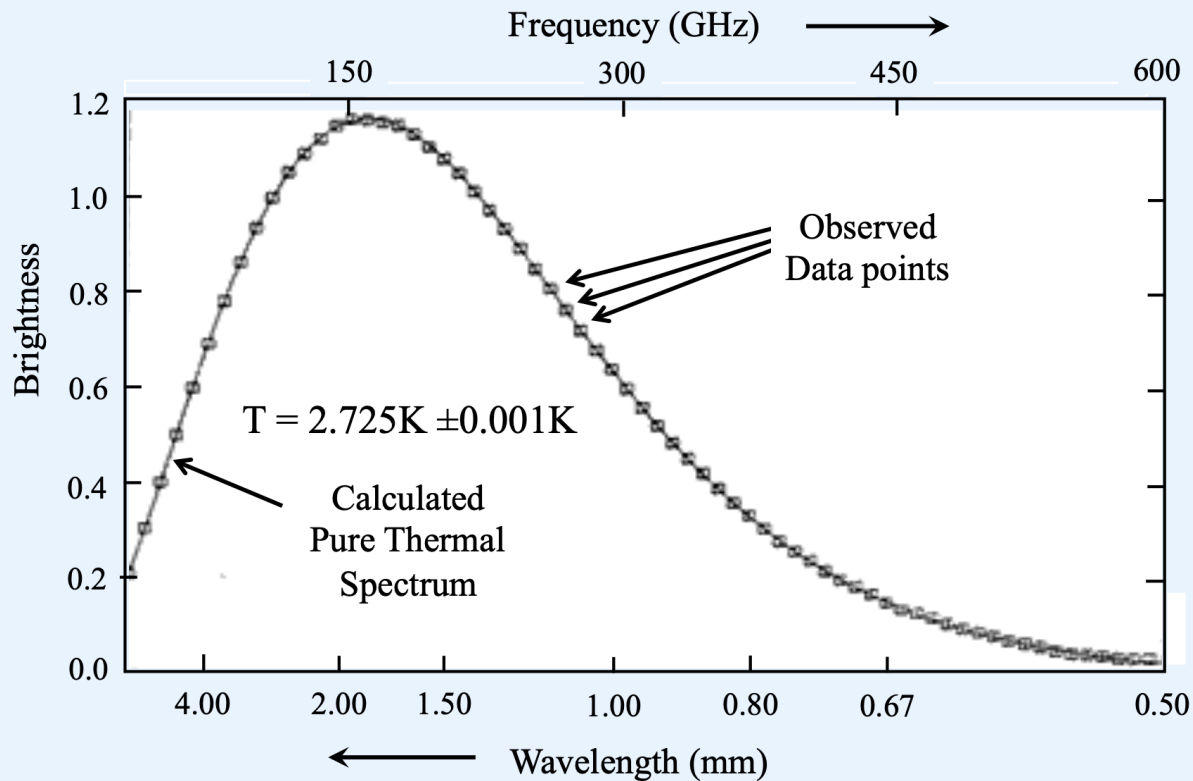
Cosmic Background Explorer (COBE)



- Far-Infrared Absolute Spectrophotometer (FIRAS)
[PI: John Mather]
- Differential Microwave Radiometer (DMR)
[PI: George Smoot]
- Diffuse Infrared Background Experiment (DIRBE)
- Dewar with 1.4 K liquid helium
- Nobel Prize in 2006

CMB spectrum

$$u(\nu)d\nu = \frac{8\pi h}{c^3} \frac{\nu^3}{\exp(h\nu / k_B T) - 1} d\nu$$



Temperature of recombination

Naively, recombination might happen when $k_B T \sim 13.6 \text{ eV}$ (typical photon energy \sim H binding energy). i.e. $T \sim 150,000\text{K}$.

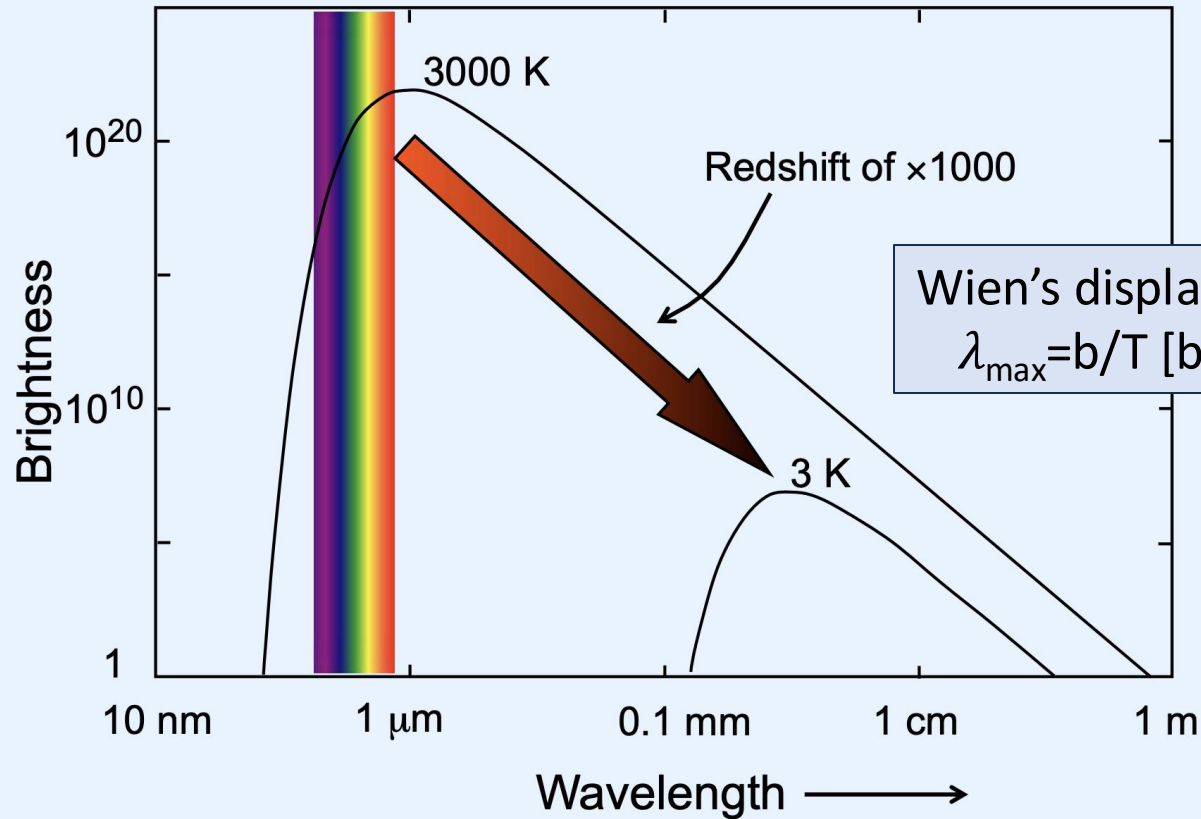
However, photons more abundant than protons, so even at lower temperature, there are many more photons with $E > 13.6 \text{ eV}$.

Photon/baryon ratio is large and preserved during expansion:

$$\frac{n_\gamma}{n_b} \approx \frac{\Omega_{\gamma,0} / \langle E_\gamma \rangle}{\Omega_{b,0} / \langle E_b \rangle} \approx \frac{5.0 \times 10^{-5} / 7 \times 10^{-4} \text{ eV}}{0.04 / 938 \text{ MeV}} \approx 1.7 \times 10^9$$

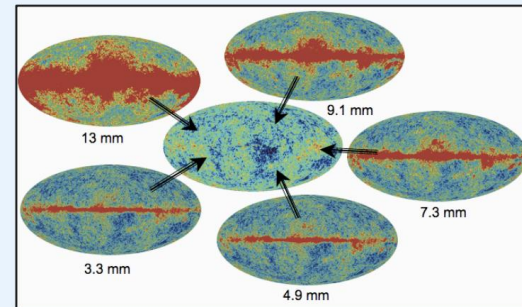
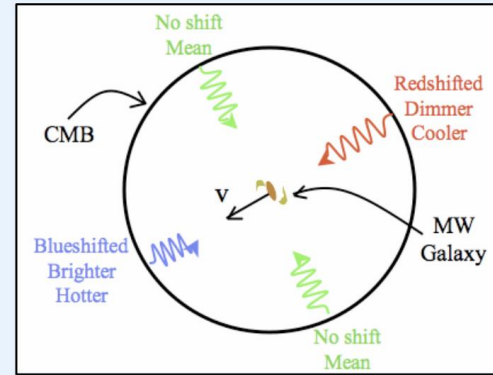
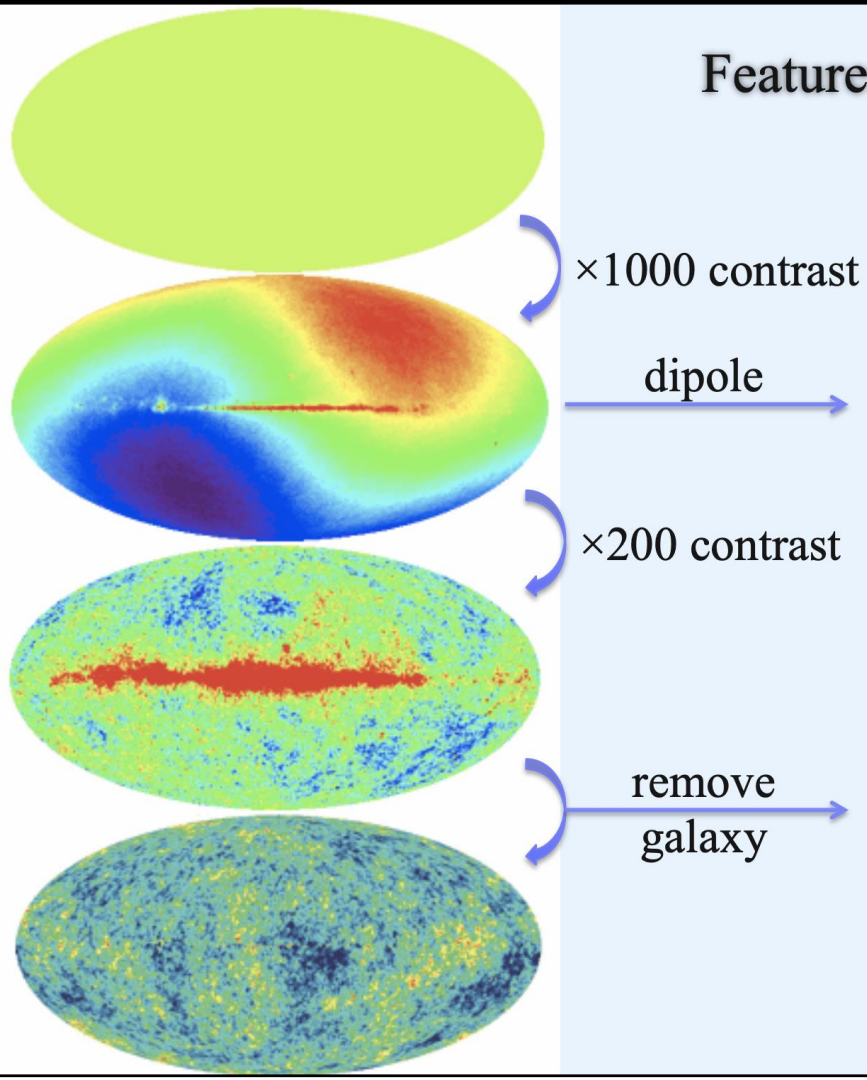
At 5700K, the tail of the black body contains as many photons with $E > 13.6 \text{ eV}$ as there are protons.

Redshift preserves blackbody spectrum with $T = T_0/a$



Wien's displacement law:
 $\lambda_{\max} = b/T$ [$b = 3 \text{ mm}\cdot\text{K}$]

Features visible in the CMB all-sky map

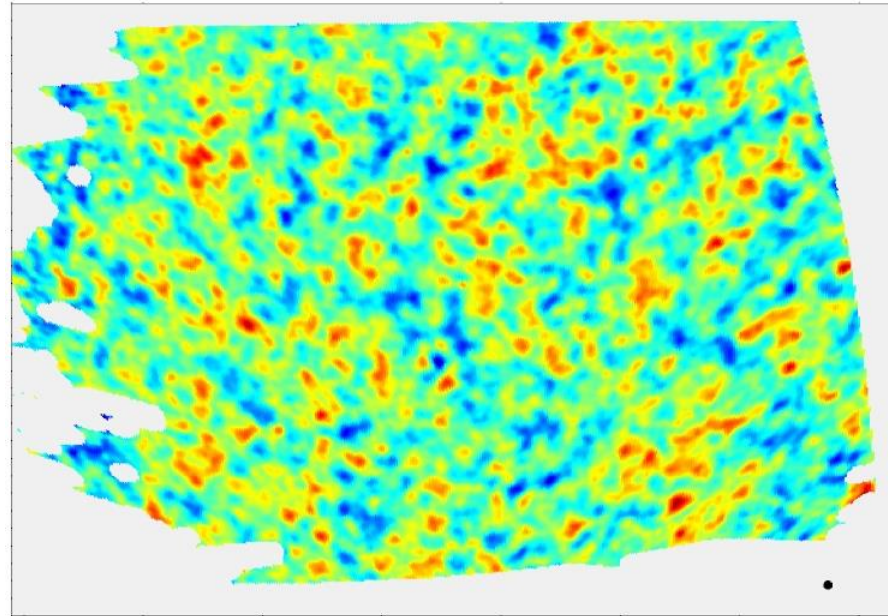


CMB anisotropies

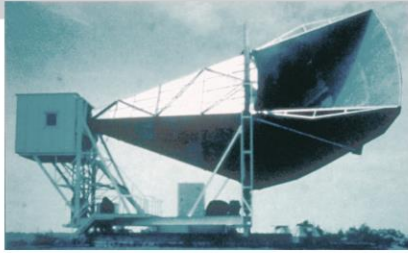
- 1997-1998, 2003 BOOMERanG experiment (Caltech + Sapienza Univ. of Rome)
Balloon Observations Of Millimetric Extragalactic Radiation and Geophysics

Flew 42 km high above Antarctica

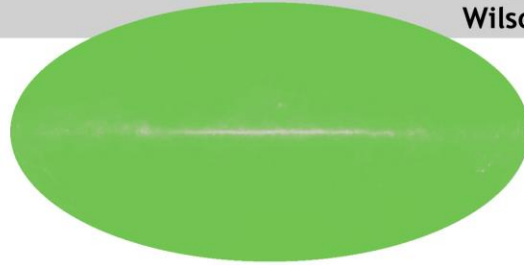
-300 μK -300 -200 -100 0 100 200 300 μK



1965



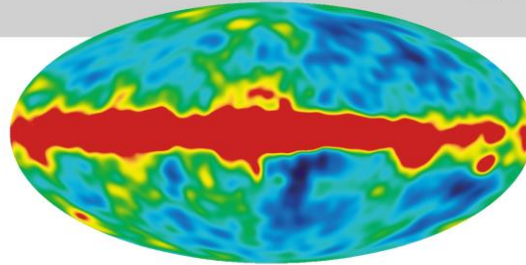
Penzias and
Wilson



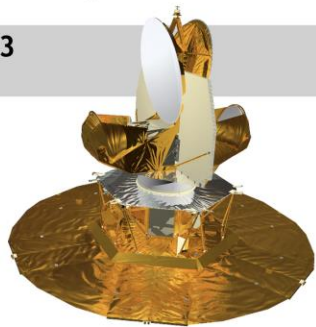
1992



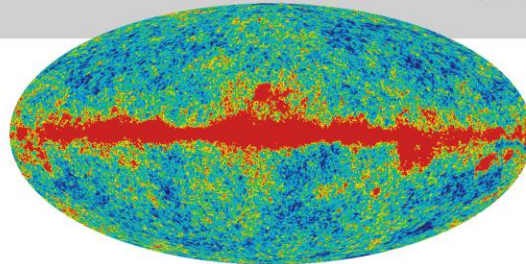
COBE



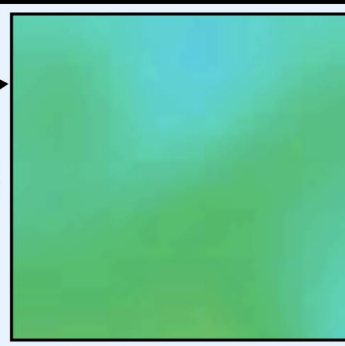
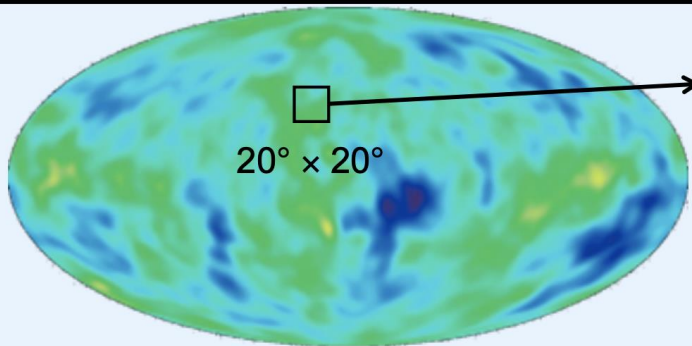
2003



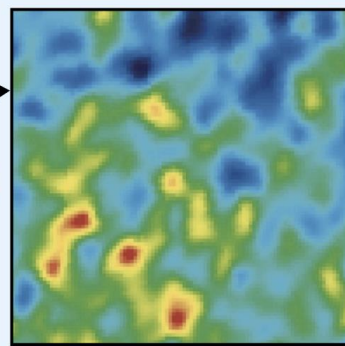
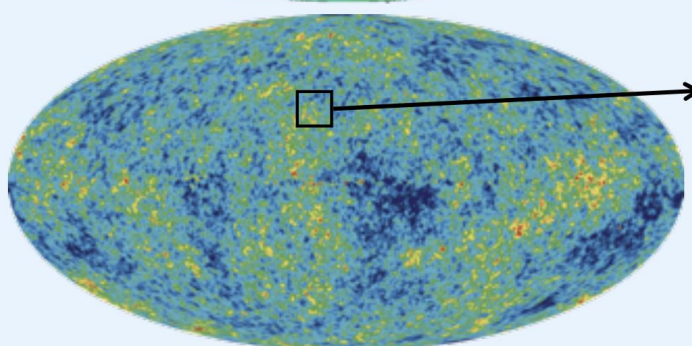
WMAP



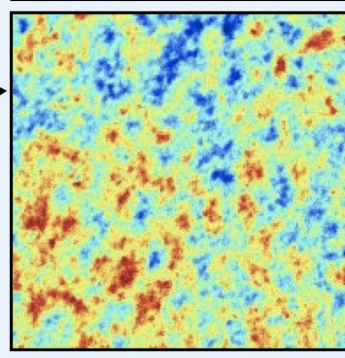
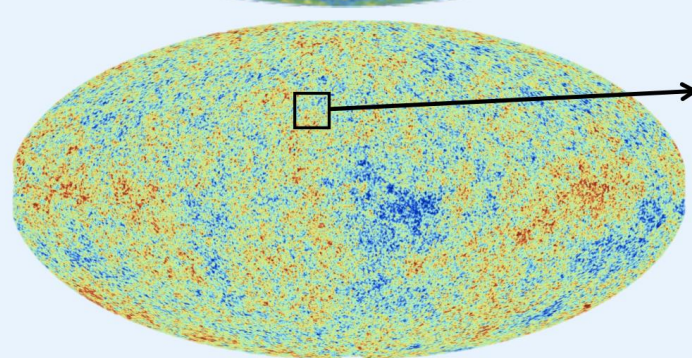
Wilkinson Microwave Anisotropy Probe (WMAP), 2001-2010



COBE: 1990
Resolution: 7°
Sensitivity: ×1
Cost: 600 M\$

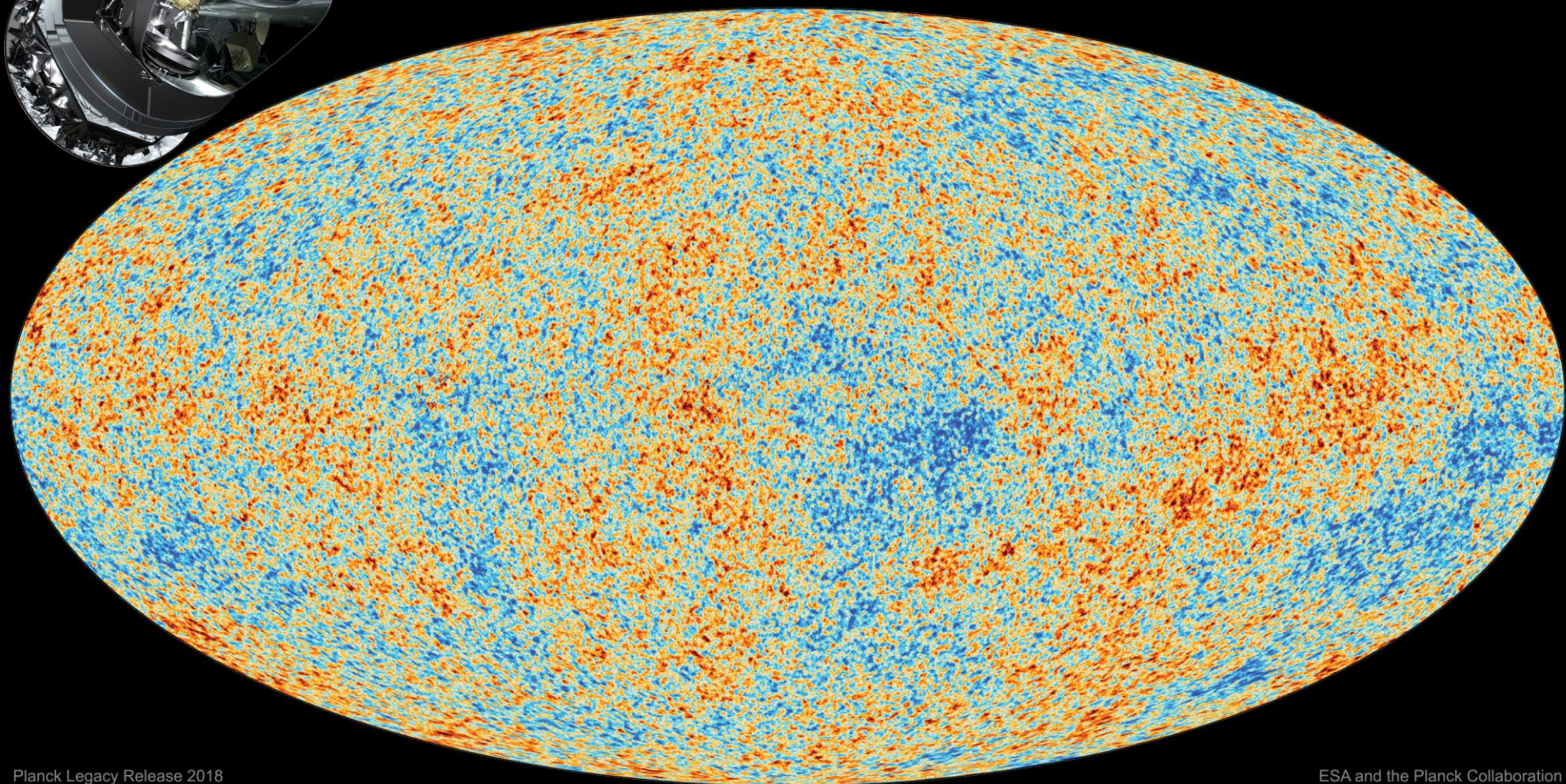
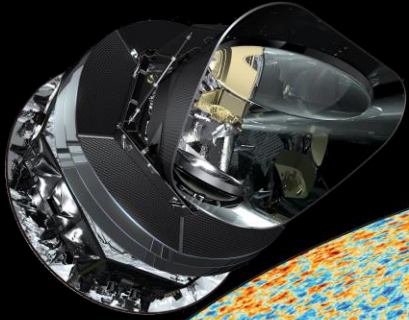


WMAP: 2003
Resolution: 0.13°
Sensitivity: ×5
Cost: 800 M\$



Planck: 2012
Resolution: 0.08°
Sensitivity: ×15
Cost: 1000 M\$

Planck Satellite (ESA, 2009-2013)



Spherical Harmonics

Any quantity which varies with position on the surface on a sphere can be written as the sum of spherical harmonics:

$$\frac{\Delta T}{T}(\theta, \phi) = \sum_{l,m} a_{lm} Y_{lm}(\theta, \phi)$$

measured anisotropy map as function of spherical polar angles θ and ϕ

weight - how much of the signal is accounted for by this particular mode

spherical harmonic function

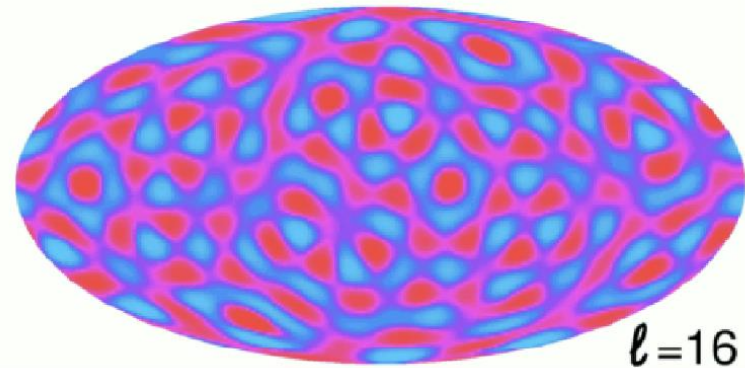
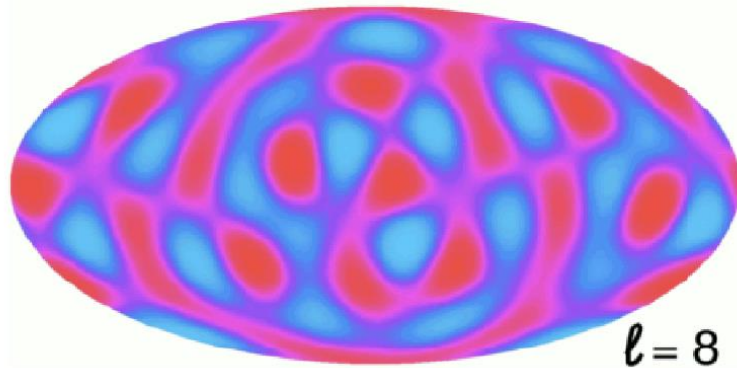
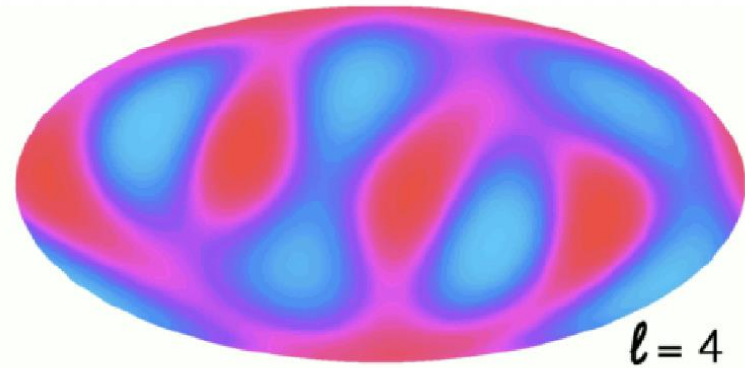
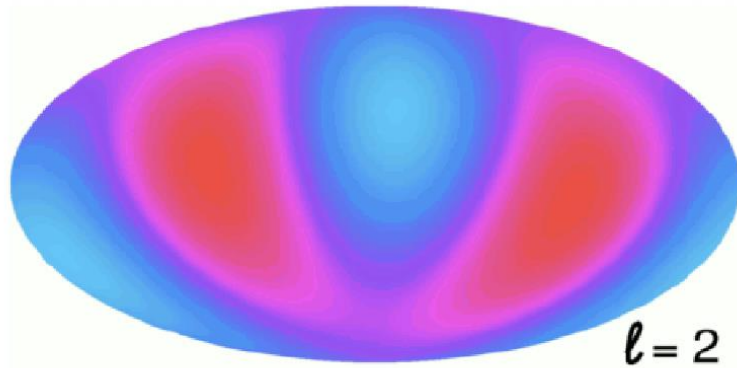
The spherical harmonic functions themselves are just increasingly complicated trigonometric functions, e.g.:

$$Y_{22}(\theta, \phi) = \sqrt{\frac{5}{96\pi}} 3 \sin^2 \theta e^{2i\phi}$$

$$C(l) = \frac{1}{2l+1} \sum_m a_{lm}^2$$

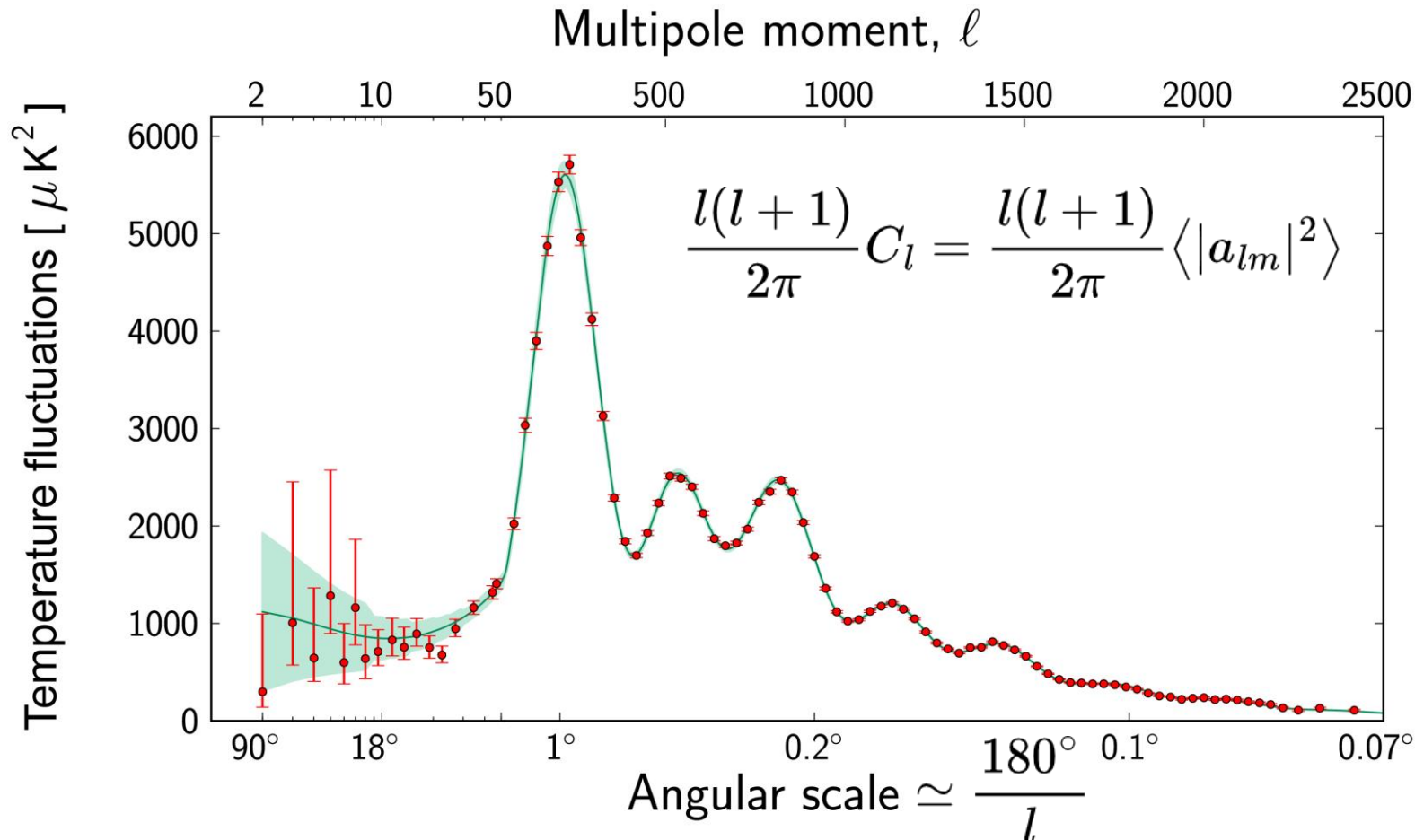
Normally plot $C(l) l(l+1)/2\pi \mu\text{K}^2$ against $l \approx 180/\Delta\theta^\circ$. This shows relative power per log l .

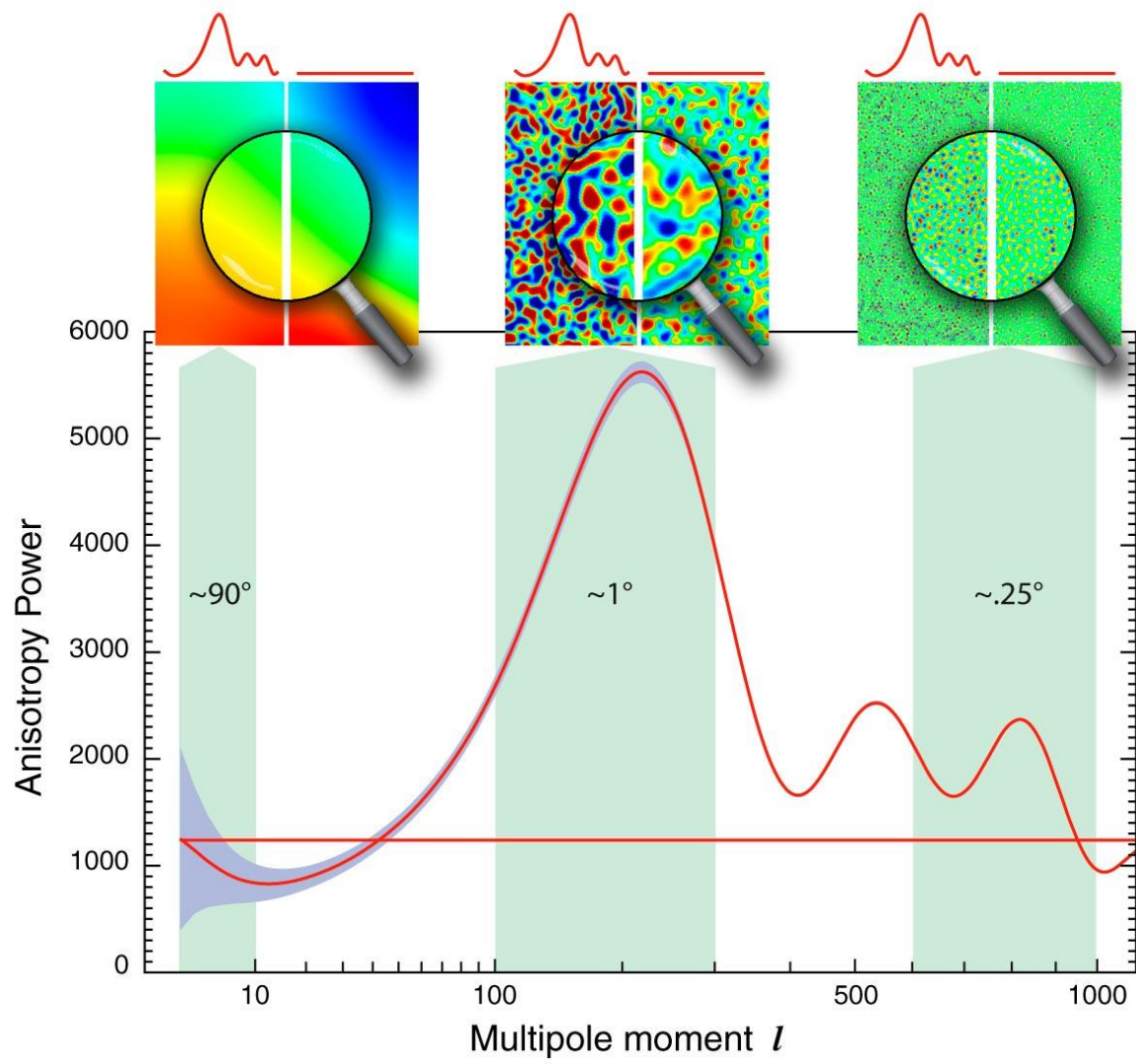
Spherical harmonic decomposition



(from N. Wright)

Planck 2018 power spectrum of temperature anisotropies





Sources of anisotropies

1. Inhomogeneities in matter density

- In baryonic matter: $\langle(\delta\rho/\rho)^2\rangle^{1/2} \sim 10^{-5}$
- In dark matter: $\langle(\delta\rho/\rho)^2\rangle^{1/2} \sim ?$ (10^{-3} at $a_*=1/(z_*+1) \sim 10^{-3}$)

2. Non-integrated Sachs-Wolfe effect

3. Acoustic oscillations

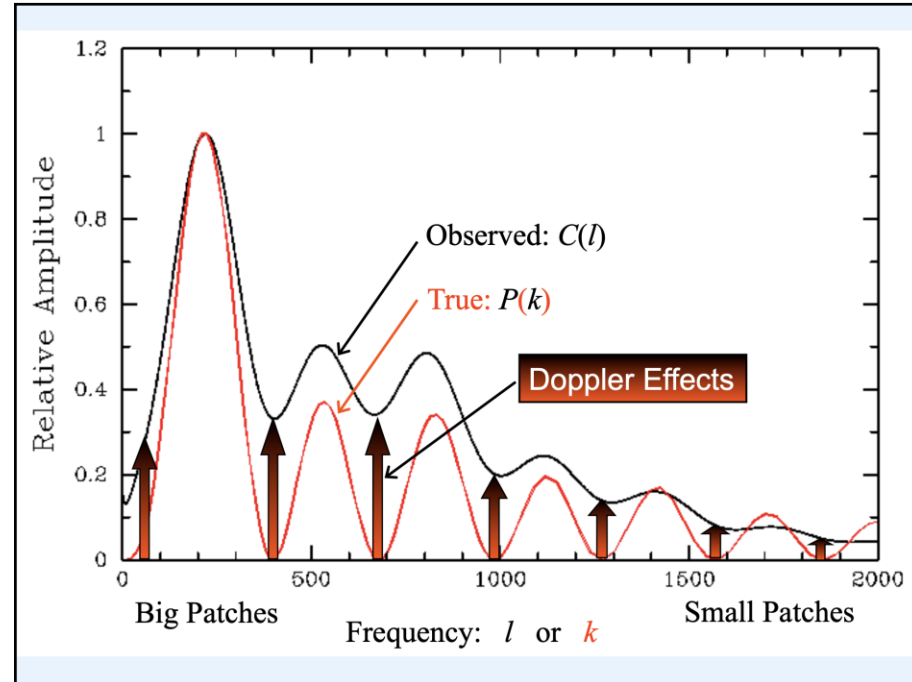
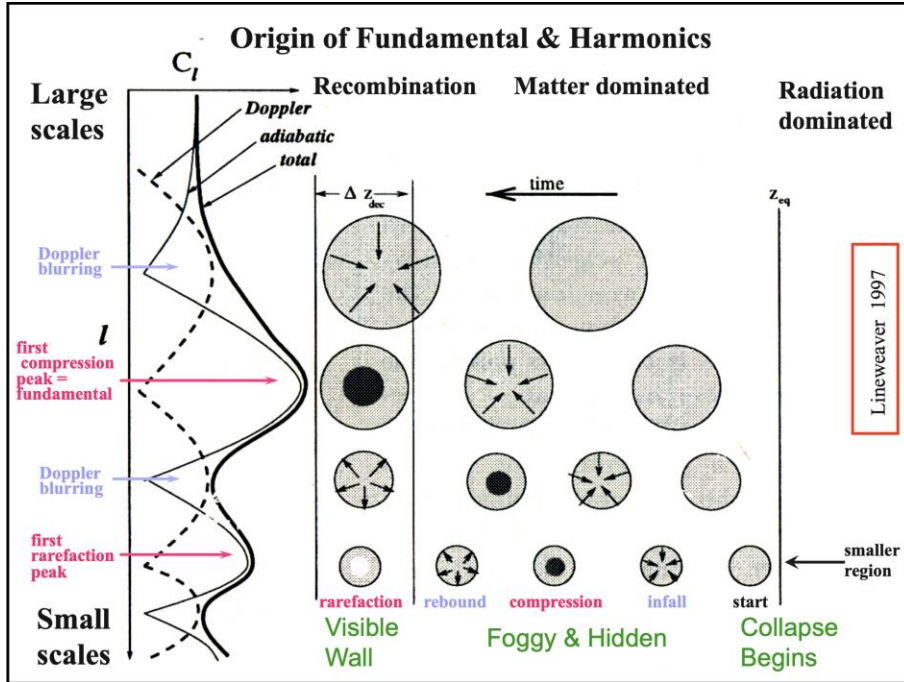
- Highest (= first) peak at $\ell = 180^\circ/\theta_*$  $\theta_* = \frac{r_s(T_*)}{d_A(z_*)}$ See extra note
[“First acoustic peak in CMB”](#)

4. Silk damping

5. Other secondary and tertiary effects

- Secondary: integrated Sachs-Wolfe effect, Sunyaev-Zeldovich effect, etc.
- Tertiary: scattering on galactic dust, point radio sources, etc.

Acoustic oscillations



Sources of anisotropies

1. Inhomogeneities in matter density

- In baryonic matter: $\langle(\delta\rho/\rho)^2\rangle^{1/2} \sim 10^{-5}$
- In dark matter: $\langle(\delta\rho/\rho)^2\rangle^{1/2} \sim ?$ (10^{-3} at $a_*=1/(z_*+1) \sim 10^{-3}$)

2. Non-integrated Sachs-Wolfe effect

3. Acoustic oscillations

- Highest (= first) peak at $\ell = 180^\circ/\theta_*$  $\theta_* = \frac{r_s(T_*)}{d_A(z_*)}$ See extra note
[“First acoustic peak in CMB”](#)

4. Silk damping

5. Other secondary and tertiary effects

- Secondary: integrated Sachs-Wolfe effect, Sunyaev-Zeldovich effect, etc.
- Tertiary: scattering on galactic dust, point radio sources, etc.

